Conceptions of experiments in teaching mathematics and teaching physics in Vietnam

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Abstract

This article presents a part of the Inter-Tetra project. This study firstly reviews the literature on conceptions of experiments in didactics of math and didactics of physics to design questionnaires to survey the conceptions of experiments in teaching physics and teaching math in Vietnam. Thereafter, the survey has been conducted among the math and physics pedagogical students in the Hanoi National University of Education (HNUE). The results of the survey have revealed the similarities and differences of the concepts of an experiment in teaching math and physics. In addition, this study also discusses the causes and consequence of the similar and dissimilar concepts of experiments.

1. Introduction

Mathematics and Physics have an intimate relationship. Not only do they complement each other, but both share the similarities in the historical development (Krause & Witzke, 2015). The interaction of mathematics and physics lead educators to implement integrated teaching of math and science (Galili, 2018). This also facilitates the teaching activities to enhance students' competency. The aim of the Inter-Tetra (Interdisciplinary Teacher Training) project is to implement the fruitful discussions about the similarities and differences between mathematics and physics in teacher training (Krause et al., 2019). In this study, we built a questionnaire based on different notions of experiments to record data about the perception of math and physics teacher students in order to find out the similarities and differences in perception of pedagogical students in these two subjects on experiments and on the way of using experiments in teaching physics and math.

2. Experiments in research and teaching

2.1. Experiments in Physics and Mathematics

Galilei and the first physicists used empirical research methods to emphasize the aspect of arbitration between arguments, while mathematicians like Gauß often approached experiments as initial symbols or a way to illustrate abstract objects (Philipp et al., 2015). Despite the similarities between these two subjects, the roles of experiments in physics and mathematics are still different due to the characteristics of each subject. The experiment in physics research plays a key role in the history of physics. The role of experiments in mathematics research has just been more apparent recently as the numerical methods and the simulation software appear.

Experiments in physics can be classified into 4 aspects: observation, measurement, the experiment itself and the epistemological role of the experiment – the so-called experimental method (Schwarz, 2009). This is quite similar to the classification of (Etkina et al. 2002) in which they stated 3 types of experiments: observational experiments, testing theory model experiments, and application experiments.

In order to have a comparison on the role of experiments in mathematics and in physics, we base on two typical notions which are shown the table 1.

<table>
<thead>
<tr>
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<tbody>
<tr>
<td>1. Observational experiment: The goal is to observe a new phenomenon. Students later devise explanations for the observations.</td>
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<td>2. Testing experiment: The goal is to test whether the explanation devised for some observed phenomenon works. Students use explanations that they constructed for type 1 experiments to make a prediction about the outcome of a new experiment.</td>
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<tr>
<td>3. Application experiment: The goal is to apply the explanation that has been tested in type 2 experiments to explain new phenomena</td>
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<tr>
<td>1. Gaining insight and intuition.</td>
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<td>2. Discovering new patterns and relationships.</td>
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<tr>
<td>3. Using graphical displays to suggest underlying mathematical principles.</td>
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<tr>
<td>4. Testing and especially falsifying conjectures.</td>
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<tr>
<td>5. Exploring a possible result to see if it is worth formal proof.</td>
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<tr>
<td>6. Suggesting approaches for formal proof.</td>
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<tr>
<td>7. Replacing lengthy hand derivations with computer-based derivations.</td>
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<tr>
<td>8. Confirming analytically derived results.</td>
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</tbody>
</table>
or to design technical devices.

Tab. 1: Conception on experiments in physics and mathematics

Borwein (2008) also notes that the above activities are quite similar to the role of laboratory experimentation in the physical and biological sciences, especially “computational experimentation” in physical science and engineering.

2.2. Role of experiments in physics teaching and mathematics teaching

In teaching physics, an experiment is an indispensable medium. This is not only reflected in textbooks but also in any literature on the didactics of physics. The experiment is always considered as a multi-purpose tool bringing high value for learning.

Besides, it is quite unusual to integrate experiments into teaching math. The number of articles applying experiments in teaching math is still limited. There are two ways to use experiments in teaching math. The first form is experimental mathematics, the numerical method and simulation software. The second form is using hands-on mathematics — like „Mathematik zum Anfassen” (Beutelspacher, 2018).

In the first approach from Jinyuan-Li (2003), it is recommended that the following steps can be used to apply experiments into math teaching:

- set out from some practical examples (including examples designed by students themselves)
- do experiments on the computer
- find out the rules among them
- make abstractions
- verify and prove your abstractions

In the second approach, experiments in teaching maths are homologous with exploration experiments or hands-on experiment in physics, though Beutelspacher (2018) distinguishes mathematics from sciences such as physics or chemistry, where experiments are used to verify a theory or to falsify a wrong hypothesis. Also, mathematical experiments are not used to simply illustrate a definition or a theorem. The role of a mathematical experiment works “bottom-up”; starting from experience, leading to insight. It is an impulse. If the experiment is good, this impulse is so strong that it enables the visitor to ask the right questions, to get the right conceptions and, finally to get by an ”Aha-moment” the right insight.

In reality, teachers also take some experiments or retell some illustrative experiences as teaching students some math topics at elementary and junior high schools (Beutelspacher, 2018). Hamiltons’ Icosian Game, the ”Tower of Hanoi” and the Soma cube - Hein or tessellation (Ilucová, 2006), are examples of such types of experiments.

In some cases, math teachers also use experiments for testing the hypothesis or for theoretical reasoning. For example, to find the relationship between the height of a person and the length of footsteps when walking (Axel & Michael, 2015).

Thus, we see that the conception of experiments in mathematics and physics are quite similar (in a simulated experiment, illustrated experiment) but there are still many differences. In order to detect how these conceptions of experiments affect pedagogical students, the specific research questions are:

Is there a difference between conceptions about the experiment (definition, role, a necessity in teaching) of physics and math pedagogical students?
Is there a difference between conceptions about the experiment (definition, role, a necessity in teaching) of students before and after studying didactics of their subjects?

3. Method of study

3.1. Context

The HNUE is one of the biggest and oldest universities in Vietnam, training teachers and lecturers in educational research. Most of researchers in physics and math education in Vietnam before 2000 were considerably influenced by the Soviet education because almost all of them studied there. In recent years, the German education have also been conveyed with a source of staff studied in Germany. Despite the trend of globalization as well as the comfort in accessing information resources with the diversity of education perspective, the current researches of mathematics and physics in Vietnam have still influences and thereby have many similarities with the kind of teaching in Germany.

For that reason, the physics pedagogical students at the HNUE are fully trained and have similar views on the use of experiments in teaching physics. Besides, the use of experiment in teaching math is just quite a bit mentioned in the studies of math teaching (Trần, 2009). Now a few students have reached to hands-on math through open math days with active participation of several private STEM math or education centers (Pomath-center).

It is noticed that math has always been considered a “king subject” in Vietnam for a long time, the best students will choose math and the entrance exam to the mathematics department of HNUE is always the most demanding among the universities in Vietnam.

3.2. Sample selection

Because the curriculum in HNUE is in the parallel model in which students will study the subjects of fundamentals of teaching of math and science in the 2nd and 3rd year, we choose first-year students (before being taught the fundamentals of teaching) and the third-year student (after studying the fundamental of teaching) to attend the survey (tab. 2).
3.3. Questionnaire (see Appendix)

The questionnaire is designed based on two notions. The first one is the theory about conceptions about experiments in mathematics and in physics. The second one is the experiences of the authors including observations and answers of short interviews with teachers and students through the following questions:

• What is an experiment?
• What functions do experiments perform in teaching?
• Tell about an experiment which is most impressive to you as a student.

Based on these, we discussed and clarified that there are six possible conceptions about experiments as follows.

1. Experiment as a part of a scientific method
2. Experiment as a way for proving a hypothesis
3. Experiment as a measurement for inducing a new law
4. Experiment as a simulation or demonstration tool
5. Experiment as a game
6. Experiment as a trial activity

Each of these perspectives was made explicit in the items in the questionnaire (see appendix). With the question number 3, the sentences corresponding to the types of conceptions are: item 1 for type 1; item 5 and item 9 for type 2; item 4 and item 7 for type 3; item 3, item 6 and item 8 for type 4; item 9 for type 5; item 2 for type 6.

With the question number 4, we coded by clarifying the students’ conceptions given in the 6 types above. In the case that the students give a definition that coincides with two or more of the above conceptions, we take the most obvious conception or the conception first recorded by the student as a student’s conception.

On the other hand, these conceptions have shown the reliability with open answers and tasks that require students to draw the most impressive experiment. From the students’ answers, we classify students’ perception of an experiment according to the 6 conceptions as above.

The questions 5 and 6 go into students’ perspective about the importance and function of experiments in teaching physics and teaching mathematics.

4. Results and conclusion

4.1. Comparison of conceptions of experiment between math and physics students

4.1.1. Conceptions of experiment

About the conceptions of experiments, the result of the frequency of selection and data analysis shows that the conceptions of physics and math students are different on items 1, 4, 5, 8, and 10. Besides, we find out that students in the two faculties do not agree in the conception of considering an experiment as a part of the scientific method and as a simulation and demonstration tool. Physics students tend to treat an experiment as a part of the scientific method and a way of proving a hypothesis. Meanwhile, math students tend to consider experiments as the first step of the cognitive process or as just a trial and error method. Taking the data of question number 4, the frequency of the choice of the definition according to the types of experiments between the math and physics students is also distinctive with the results which are revealed in Fig. 1.

![Fig. 1: Comparison of frequency distribution of selecting the type of experiment of math (green) and physics (blue) students.](image)

4.1.2. Role of experiments in teaching

There is no difference between the first-year physics student and the first-year math student. Based on what is shown in question number 5, we draw a conclusion on the students’ perspectives for the necessity of experiment in teaching.

Both math and physics students think that the use of experiments in physics is more crucial than in mathematics and there is no statistically significant difference in the results of this perspective of math and physics pedagogical students (tab. 3).
Frequency of attribution about students

Regarding the conception of experiment in teaching almost have no differences of perspective in functions of helping students understand the lesson, illustration the knowledge, improving hands-on skills, developing physics thinking. Meanwhile, the belief in the function of engaging students, checking the hypothesis and consolidating the belief of the experiment in teaching are significant different between two groups (p < 0.01). Just only the belief of students in the function of mathematics thinking is decreased (p < 0.05).
The Role of Experiments in Teaching

4.2.2. The Role of experiments in teaching

With the selection of students about the role of an experiment in teaching, we can find that students from 1st year and 3rd year are not a statistically significant difference. Their perception about the function of the experiment doesn’t change in positive trend after studying subjects didactics (tab. 6). After studying subjects didactics, 3-year students just believe more in the rolls “engage” and “check the prediction” but less in the roll “develop mathematical thinking” (tab. 6).

Tab. 6: Selection of students about roll of experiment before and after studying subjects didactics

Table: Selection of students about roll of experiment before and after studying subjects didactics

<table>
<thead>
<tr>
<th>Role of experiment</th>
<th>1st year students</th>
<th>3rd year students</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deepen the student's knowledge</td>
<td>21 (61.8)</td>
<td>37 (65.7)</td>
</tr>
<tr>
<td>Engage the students more</td>
<td>13 (36.8)</td>
<td>16 (27.4)</td>
</tr>
<tr>
<td>Students would learn more</td>
<td>13 (36.8)</td>
<td>21 (36.3)</td>
</tr>
<tr>
<td>Check the prediction</td>
<td>10 (27.0)</td>
<td>11 (18.6)</td>
</tr>
<tr>
<td>Improve hands-on skills</td>
<td>10 (27.0)</td>
<td>8 (13.3)</td>
</tr>
<tr>
<td>Develop mathematical thinking</td>
<td>12 (33.3)</td>
<td>15 (26.3)</td>
</tr>
<tr>
<td>Develop physics thinking</td>
<td>11 (30.6)</td>
<td>20 (33.9)</td>
</tr>
<tr>
<td>Get students to believe in knowledge</td>
<td>16 (44.1)</td>
<td>21 (36.3)</td>
</tr>
</tbody>
</table>

Conceptions of experiments in teaching mathematics and teaching physics in Vietnam

5. Conclusion

There is a difference in the perception of math and physics pedagogical students on an experiment. Physics students have the notion of considering an experiment almost as a part of the scientific method, and a way to check the hypothesis, while math students often emphasize the functions of illustration, experience and simulation. There is no difference in the awareness of year 1 and year 3 students about an experiment, the fundamental theory of teaching subjects just help students understand the diversity of the experiment but not have the impact in changing students’ conceptions on experiments. STEM integration requires physics and math pedagogical students to have the same conceptions about using experiments. A clear idea of experiments is an indispensable part of the scientific foundation for teacher students in mathematics and physics.

6. Literatur


Acknowledgment:
To conduct this study, the research team would like to thank the pedagogical students who participated in the survey. The project is implemented within the framework of the Inter-Tetra project, which is supported by the DAAD (German Academic Exchange Service) with funds from the Federal Ministry for Economic Cooperation and Development.

Appendix: Perspectives of Experiments in Teaching
Below are some questions to gather demographic information. This data will not be used for any other purpose than for the research.

<table>
<thead>
<tr>
<th>Personal Information</th>
<th>Gender</th>
<th>Age</th>
<th>Department</th>
<th>Year</th>
<th>University Entrance Exam Score</th>
<th>Math</th>
<th>Physics</th>
<th>Chemistry</th>
<th>Biology</th>
</tr>
</thead>
<tbody>
<tr>
<td>Name (optional)</td>
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<tr>
<td>1. Sketch an experiment which is the most typical one in physics (explain if needed).</td>
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<tr>
<td>2. Is there any Math content considered as an experiment? If yes, please give an example (explain if needed).</td>
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<tr>
<td>3. Which of the following actions is an experiment?</td>
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<td></td>
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</table>

<table>
<thead>
<tr>
<th>Action description</th>
<th>Yes</th>
<th>No</th>
<th>Other ideas</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. Lan supposes that drinking water frequently would benefit the skin. She tests this theory as following. In the first week, she drinks water as prescription and observes the skin, following by a week in which she drinks less water and observes the skin again. Then she compares the results between the two weeks.</td>
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<tr>
<td>2. Lan goes to Hoa’s house to take something for Hoa. So Hoa gives Lan her set of keys to open the door. Lan tries the keys one by one to get in the house.</td>
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<tr>
<td>3. Lan tries to solve a problem calculating the velocity of a jumping parachutist. Lan applies different ways using different knowledge and manners such as computer modeling and formula transformation.</td>
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<tr>
<td>4. Lan rolls the dice to find out the rule that if we roll the dice so many times, it will be approximately the same probability for each face to perform.</td>
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<tr>
<td>5. From the Pythagoras’ theorem ( a^2 + b^2 = c^2 ), Lan deduces that if we cut 3 squares having the sizes a, b, and c, respectively, from the same sheet and then weigh all of them, the mass of the c-size square is equal to the sum of the other two masses. Lan conducts the experiment to test and draws this conclusion.</td>
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<td></td>
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</tr>
<tr>
<td>6. Lan solves the quadratic equation ( x^2 - 3x + 2 = 0 ) and obtains roots as ( x_1 = 1 ) and ( x_2 = 2 ). After solving, she puts the two roots ( x_1, x_2 ) back into the equation to see if they match or not.</td>
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<tr>
<td>7. From the formula of the circumference of the circle, Lan measures by the following way. She draws a lot of circles of different diameter, uses a tape to measure the diameter and circumference of the circles and then calculates the ratio between the circumference and diameter. The average value of these ratios is ( \pi ).</td>
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<tr>
<td>8. To find what the graph of equation ( y = \frac{m}{x^2} ) looks like, Lan in turn inputs different values of ( m = 1, 2, 3, \ldots ) then draws the respective</td>
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</tbody>
</table>
From the graphs, she draws a preliminary conclusion about the behavior of the graph.

9. Lan predicts that the larger the mass is, the more likely it would be sunk in water. Lan checks her prediction by putting objects of different masses in the water to see, if that is true or not.

10. In the “Math is fun” book there is a guide on how to guess the age of a friend: First, multiply your own age by 2, add the product with 5, then multiply the sum with 5. Give me your result, then I will say your age. After several tries, Lan finds out the rule is that by subtracting the first 2 digits of the result by 2, we can have correct age.

4. According to you, what is an experiment?

5. The necessity of using experiments in teaching.

6. The role of experiment in teaching
   A. Help students to understand the lesson
   B. Engage the students more
   C. Illustrate the teacher’s words
   D. Check a prediction
   E. Improve hands-on skills
   F. Develop mathematical thinking
   G. Develop physics thinking
   H. Consolidate the students’ belief on knowledge